



IEEE Int'l Workshop on Ising Machines
(Invited) 10:30~11:00, Apr. 17, 2024

Simulated bifurcation machines

Enabling NP-hard optimization-based judgement in real-time systems by quantum-inspired technology

Kosuke Tatsumura

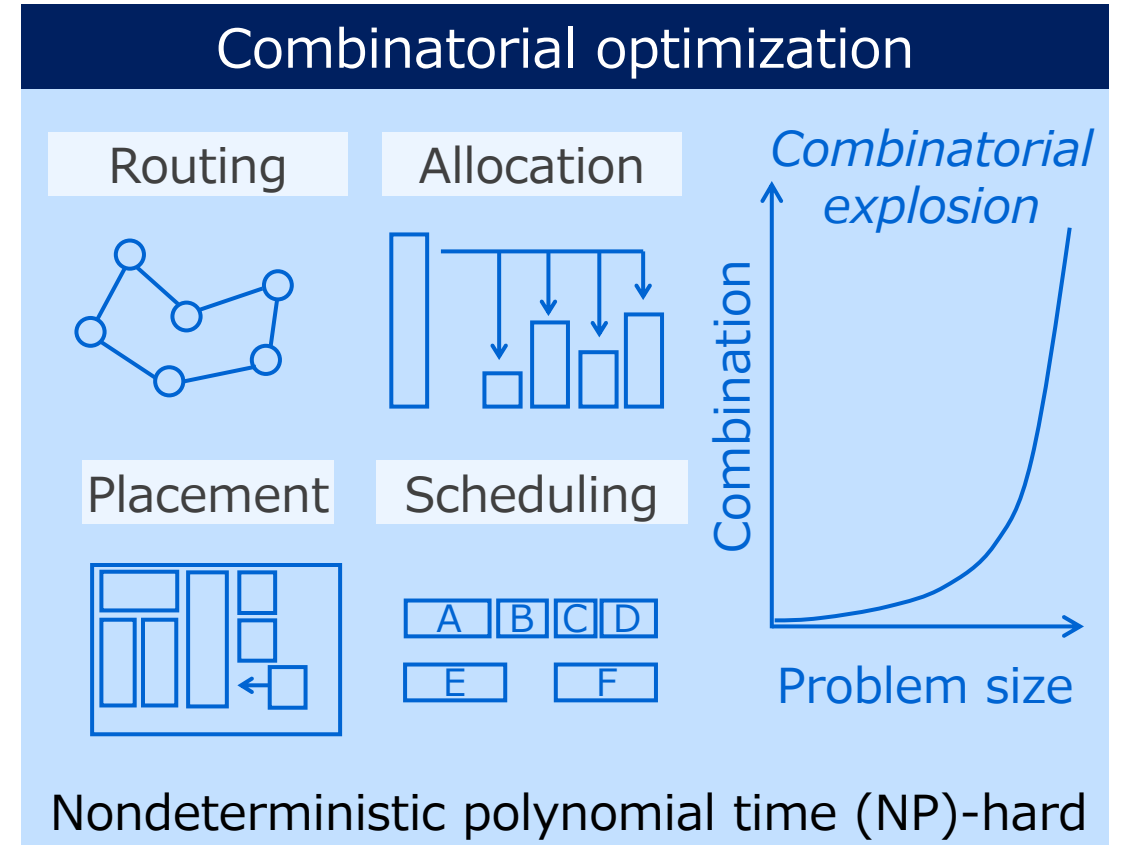
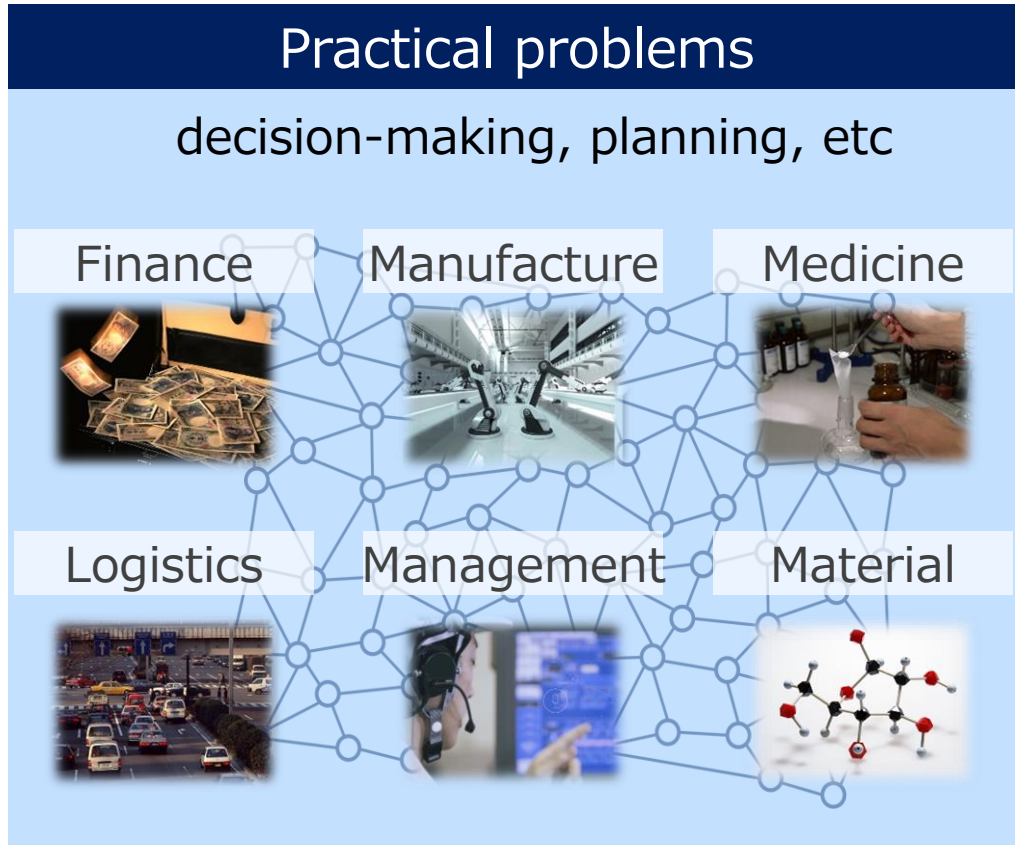
Toshiba Corporation, JAPAN

Outline

- 01 Introduction
Using quantum-inspired optimization technology in real-time systems
- 02 Simulated bifurcation machine (SBM):
theory, implementation & performance
- 03 Real-time systems with Simulated bifurcation machines (SBMs):
Finance and Automotive vehicle

Combinatorial optimization

Economically important but computationally hard



From the viewpoint of system engineering:

Making *rational* judgment in the situation/at the moment

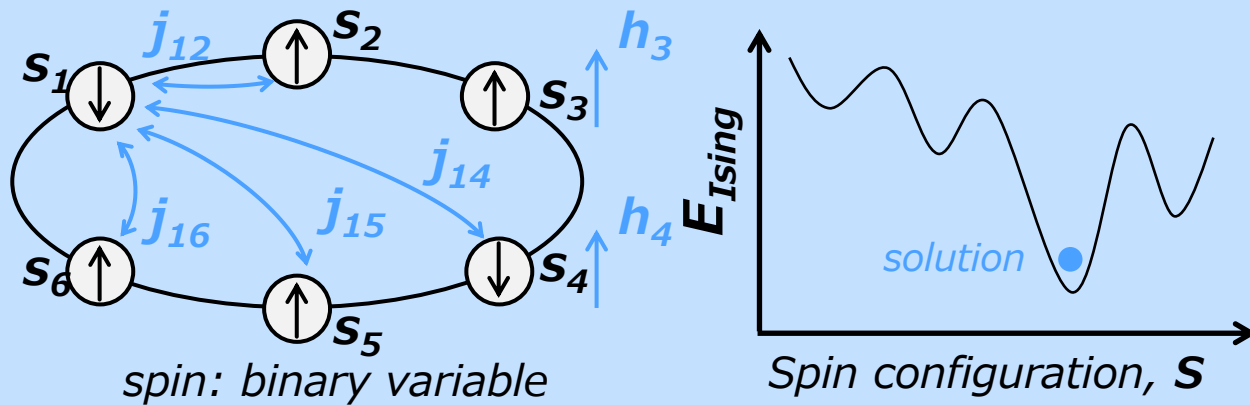
Ising machine

Special-purpose computer for combinatorial optimization

Ising problem

search for the lowest- E state of Ising model

$$E = - \sum \mathbf{j}_{ij} s_i s_j + \sum h_i s_i$$



↑ Mapping#1

Combinatorial optimization
(Quadratic discrete optimization)

Ising machines

Quantum annealer*1
(2011)



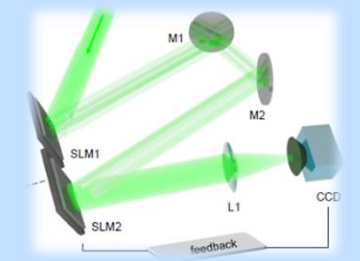
CMOS annealer*2



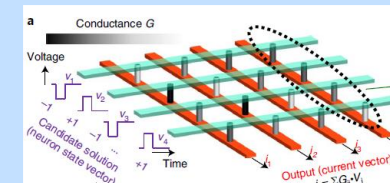
Digital annealer*3



Optical Ising machines*4,5



Memristor HNN*6



and more ...

+ Simulated bifurcation machine (2019)

*1 <https://www.dwavesys.com/d-wave-two-system>

*2 <https://www.hitachi.co.jp/New/cnews/month/2019/02/0219.html>

*3 <https://www.fujitsu.com/global/about/resources/news/press-releases/2018/0515-01.html>

*4 <https://www.ntt.co.jp/news2017/1711e/171120a.html>

*5 D. Pierangeli, et al., *Phys. Rev. Lett.* **122**, 213902 (2019).

*6 F. Cai, et al., *Nature Electronics* **3**, 409 (2020).

Quantum-inspired optimization technology

- *1 [H. Goto et al., Sci. Adv. 5, eaav2372, '19](#)
- *2 [H. Goto et al., Sci. Adv. 7, eabe7953, '21](#)
- *3 [K. Tatsumura et al., Nat. Ele. 4, 208-217, '21](#)
- *4 [T. Kashimata et al., IEEE Access 12, '24](#)

Simulated Bifurcation Machine, SBM

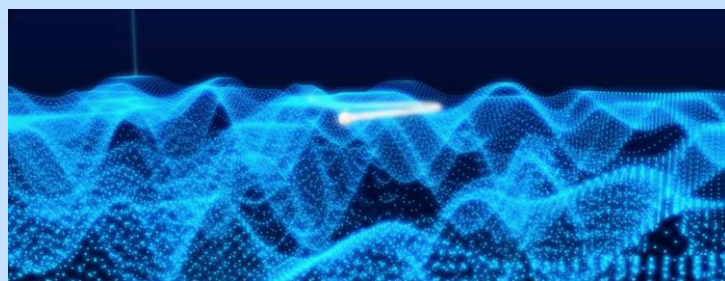
Algorithm

Quantum-inspired

Quantum bifurcation machine
in a quantum principle



Simulated bifurcation algorithm
in a new classical principle



Highly parallelizable

Implementation

High performance*^{1,2}
single-chip



Scalable*^{3,4}
multi-chip



Application

Very practical

edge/embedded

cloud



Innovative

ex. real-time systems



Edge application of SBM

Simulated bifurcation machine

*1 K. Tatsumura et al., "FPGA-Based Simulated Bifurcation Machine," *IEEE Field-Programmable Logic and Apps. (FPL)*, 2019
*2 K. Tatsumura, "Large-scale combinatorial optimization in real-time systems by FPGA-based accelerators for simulated bifurcation," *Int'l Symp. on Highly Efficient Accelerators and Reconfigurable Technologies (HEART)*, 2021

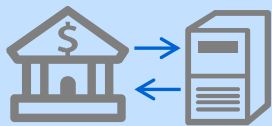
Enables real-time systems that make more rational judgments*^{1,2}

Constrains in the time domain

Real-time system

- Must respond within the critically defined time constrain
- Respond time needed for "high-speed" real-time systems:
Typically less than 1 ms
- (Conventional) simple conditional-judgement

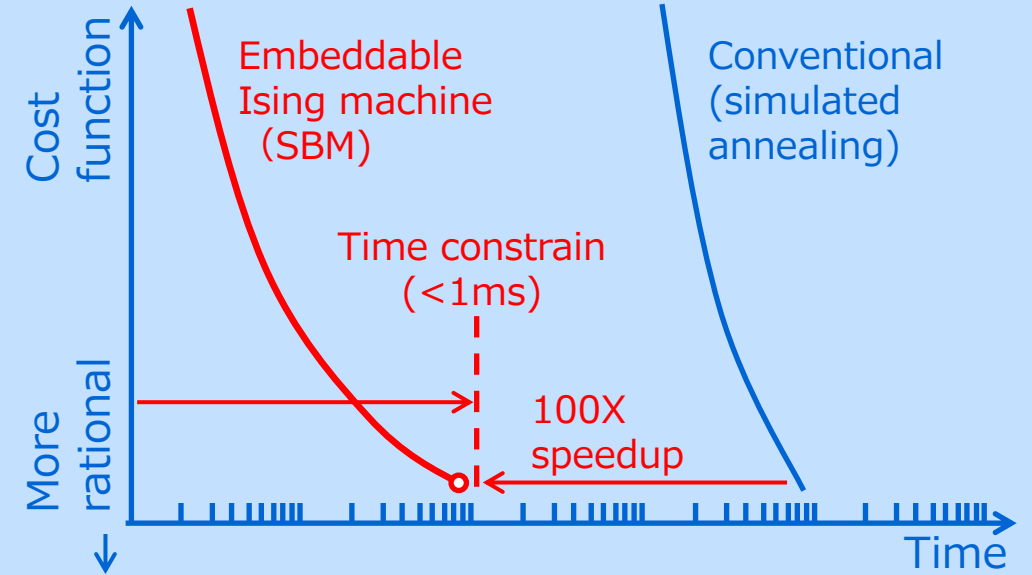
Financial trading



Automotive Vehicle

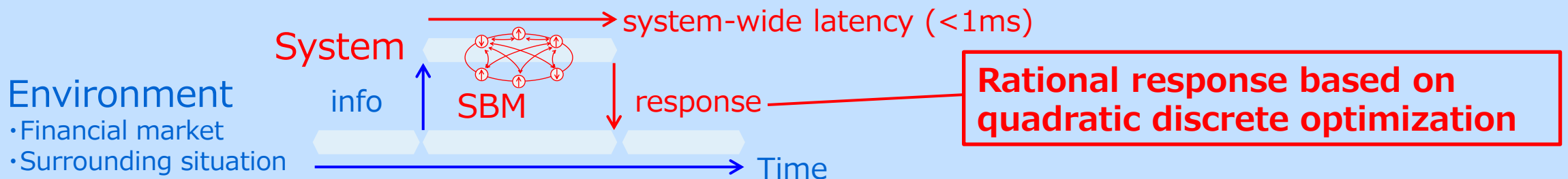


Embeddable Ising machine (SBM)



Embedding

Real-time system with embeddable SBM



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Finance and Automotive vehicle

SB theory: How it was born

*1 [H. Goto et al., Scientific Reports 6, 21686 \(2016\)](#)

*2 [H. Goto et al., Science Advances 5, eaav2372 \(2019\)](#)

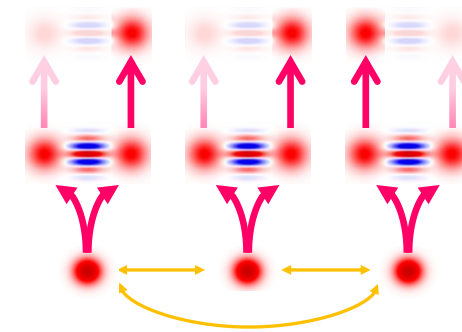
Quantum-inspired algorithm

Quantum Bifurcation (QB) machine*1

Hamiltonian describing adiabatic bifurcation process in a nonlinear oscillator network

$$H_q(t) = \hbar \sum_{i=1}^N \left[\frac{K}{2} a_i^\dagger a_i^2 - \frac{p(t)}{2} (a_i^\dagger + a_i) + \Delta_i a_i^\dagger a_i \right] - \hbar \xi_0 \sum_{i=1}^N \sum_{j=1}^N J_{i,j} a_i^\dagger a_j$$

Combinatorial optimization based on quantum adiabatic theorem



solution
quantum interference
quantum superposition
quantum bifurcation

Classical Bifurcation (CB) machine

classicization of state variables

$$H_c(\mathbf{x}, \mathbf{y}, t) = \sum_{i=1}^N \left[\frac{K}{4} (x_i^2 + y_i^2)^2 - \frac{p(t)}{2} (x_i^2 - y_i^2) + \frac{\Delta_i}{2} (x_i^2 + y_i^2) \right] - \frac{\xi_0}{2} \sum_{i=1}^N \sum_{j=1}^N J_{i,j} (x_i x_j + y_i y_j)$$

algorithmic twist for speed-up

Simulated Bifurcation (SB) algorithm (2019)*2

Classicizing QB that works in a quantum principle...?
Why SB works? What principle? **There was a discovery**

SB theory: Why it works

- *1 H. Goto et al., *Science Advances* **5**, eaav2372 (2019)
- *2 G. Finocchio et al., *Nano Futures* **8**, 012001 (2024)
- *3 H. Goto et al., *Science Advances* **7**, eabe7953 (2021)
- *4 T. Kanao et al., *Comm. Phys.* **5**, 153 (2022)
- *5 T. Kanao et al., *Applied Physics Express* **16**, 014501(2023)

New classical principle: Adiabatic and ergodic search*1

Dynamical change of energy landscape

a single local minimum



bifurcation

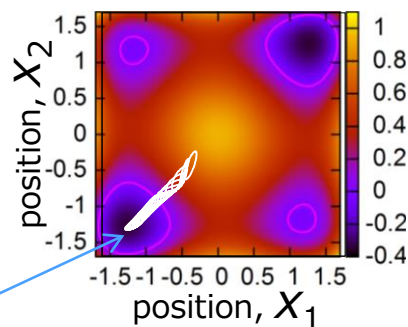
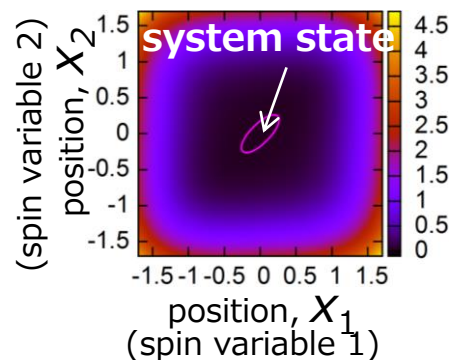
(adiabatic process)



multiple local minima (target cost function)

best solution (-1,-1)

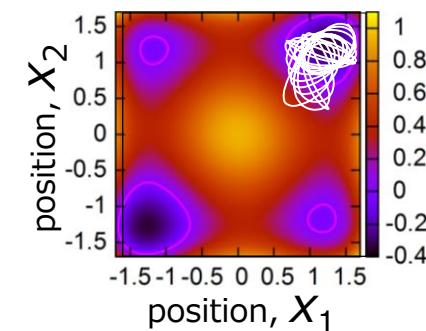
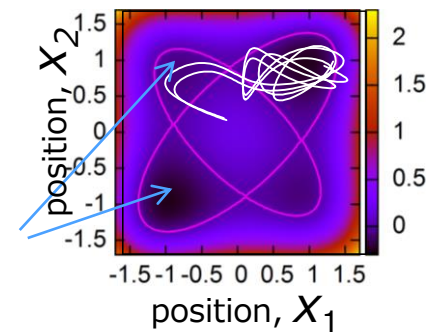
Energy landscape ($N_{\text{spin}}=2$)



adiabatic search

chase one of the minima

Multiple minima in the energetically allowable region



ergodic search

find a better one with a higher probability

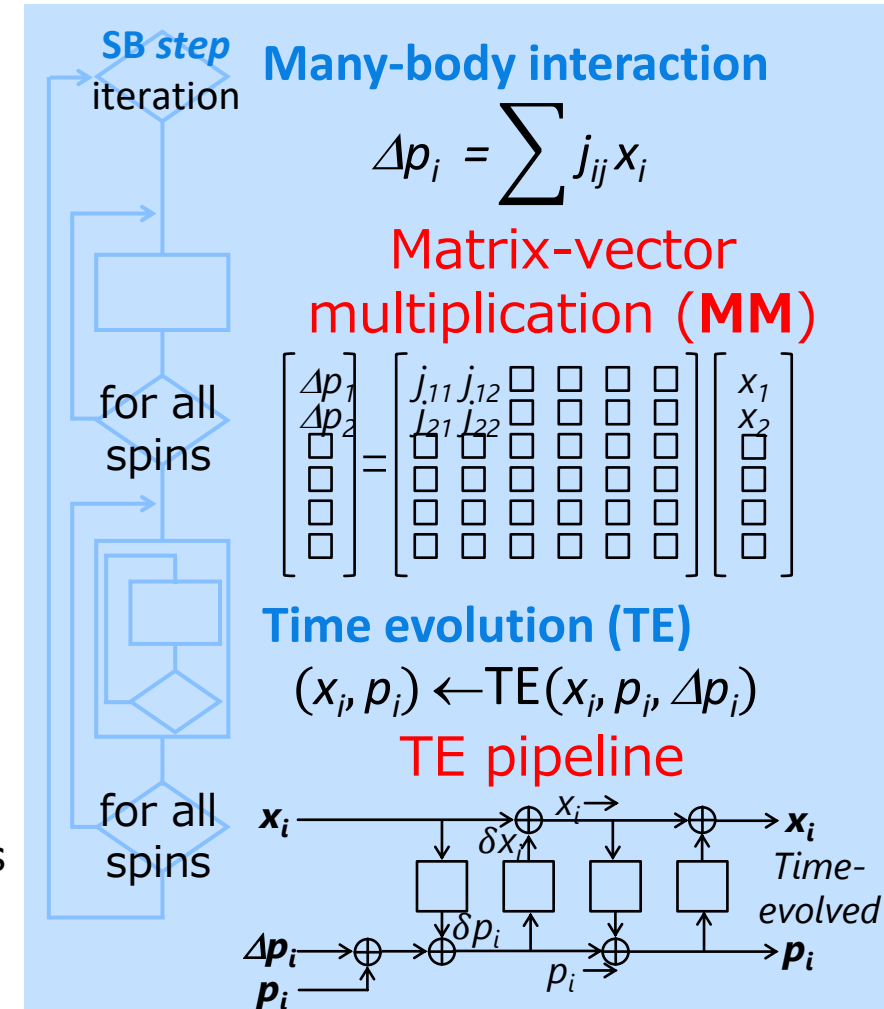
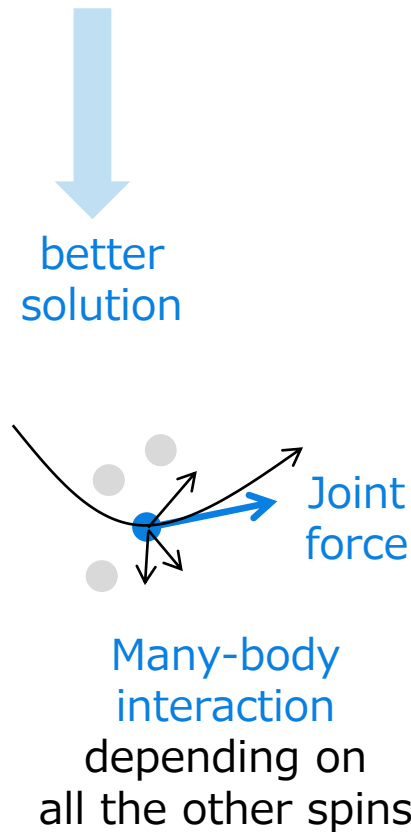
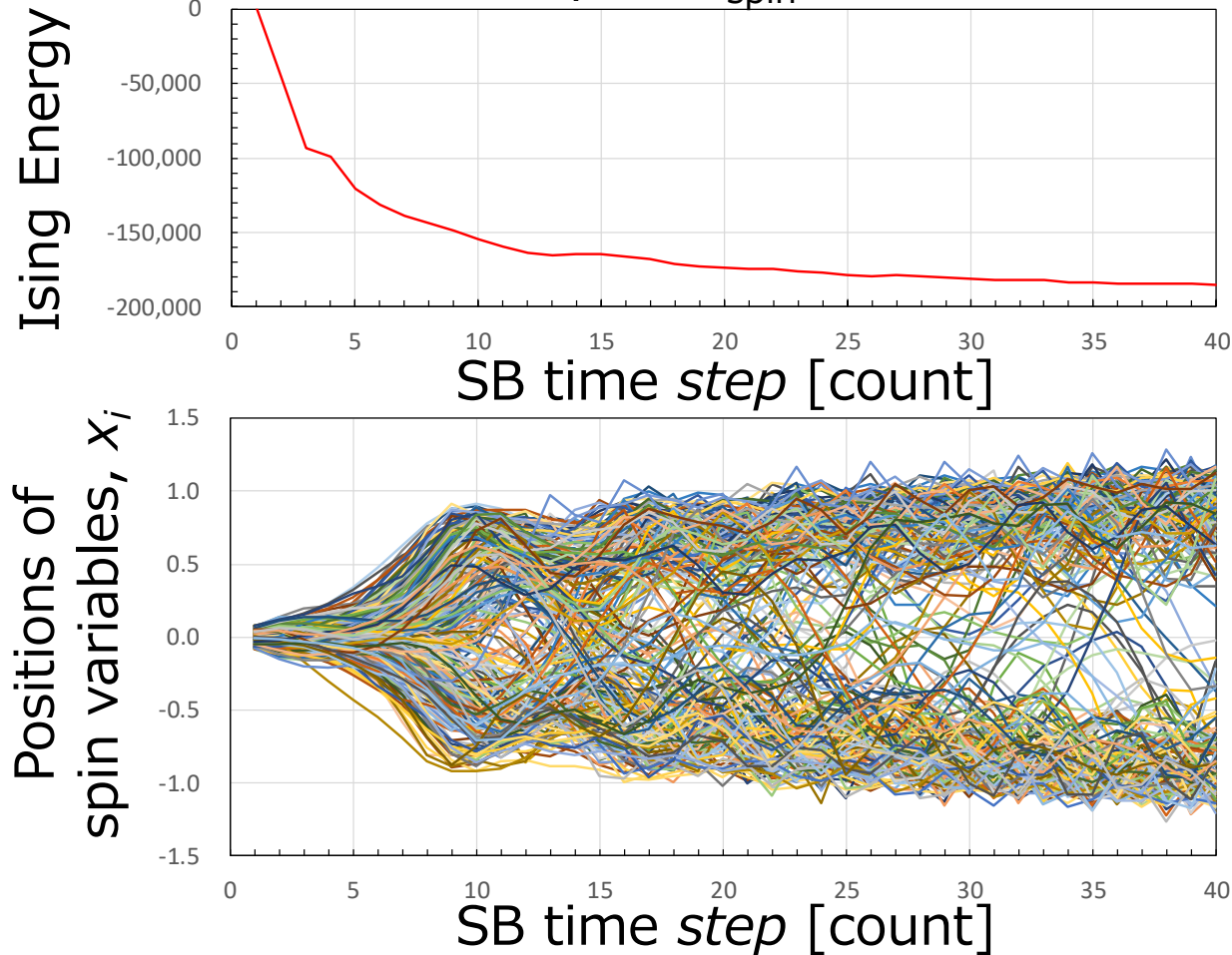
Implying *classical adiabatic theorem* (corresponding to quantum adiabatic theorem)*2 has been extended to 2nd-gen SB*3, heat-assisted SB*4, and higher-order SB*5

SB algorithm: How it works

*1 Time-evolution simulation of N -particle systems with long-range pairwise interaction, like celestial systems with gravitational interaction or molecular systems with Coulomb interaction

“ N -body”-type algorithmic structure*1 → **Highly parallelizable**

Example: $N_{\text{spin}} = 4000$



SB algorithm : Characteristics

More parallelizable than SA, Can be accelerated with **FPGAs/GPUs/NPUs**

	SA simulated annealing	SB simulated bifurcation	R-NN recurrent neural network	N-body gravitational (/Coulomb)-force
Structure	<p>Sequential updating</p>	<p>Parallel updating</p>	<p>neuron neuron</p> <p>full connection</p>	<p>position momentum</p> <p>38 FP operations</p>
Parallelism	$O(N)$	$O(N^2)$		

More parallelizable

Intensive memory access
J/W matrix (NxN matrix)

Very similar

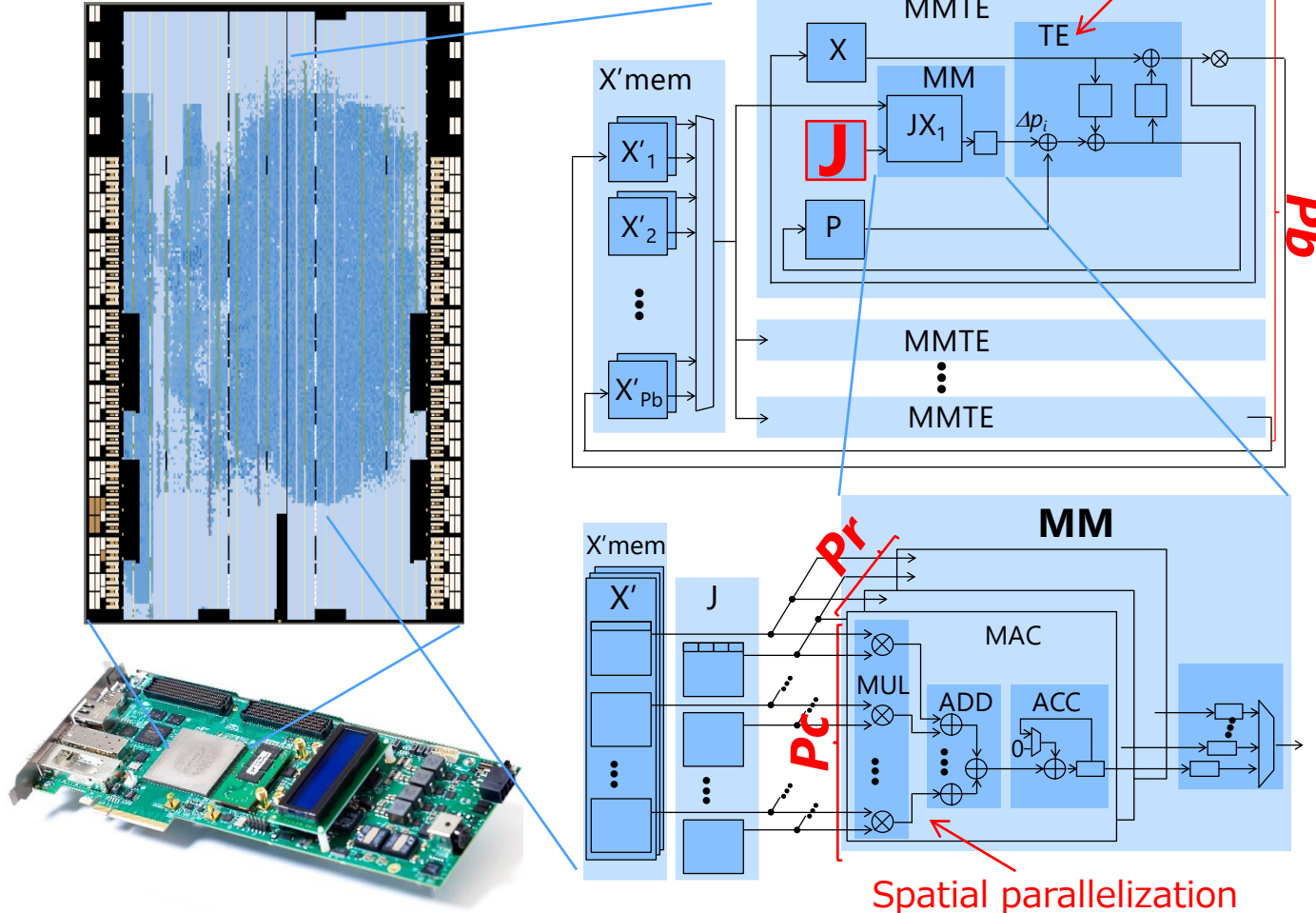
More PEs per chip
PE: pairwise interaction

SB can be accelerated with FPGAs/GPUs (not limited to special ASICs)
Many AI chips (NPUs) are beneficial also to SB

FPGA-based accelerator for SB*1

Large-scale, massively parallel, and high utilization

Arria10 GX1150 FPGA



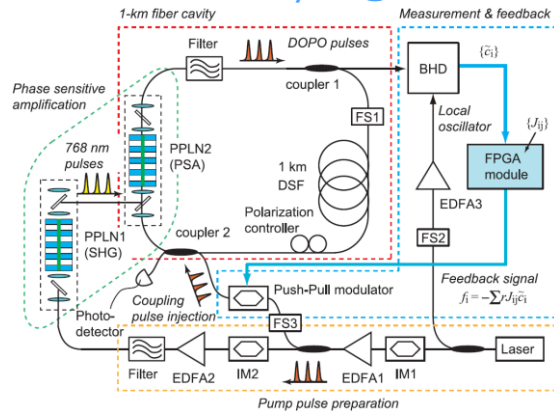
Problem	complete-graph MAX-CUT
Machine size	4,096 spins full spin-spin connectivity
Architecture	
Pr/Pc/Pb	32/32/8
# of MAC PEs	8,192
Effective activity	92%
Resource	
ALM	40%
BRAM	56%
DSP	7%
System Clock	[MHz]
Fsys	269

#PEs > N
(not achievable for SA)

Performance*1 (2019)

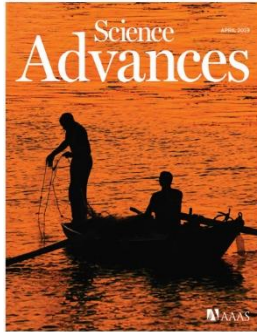
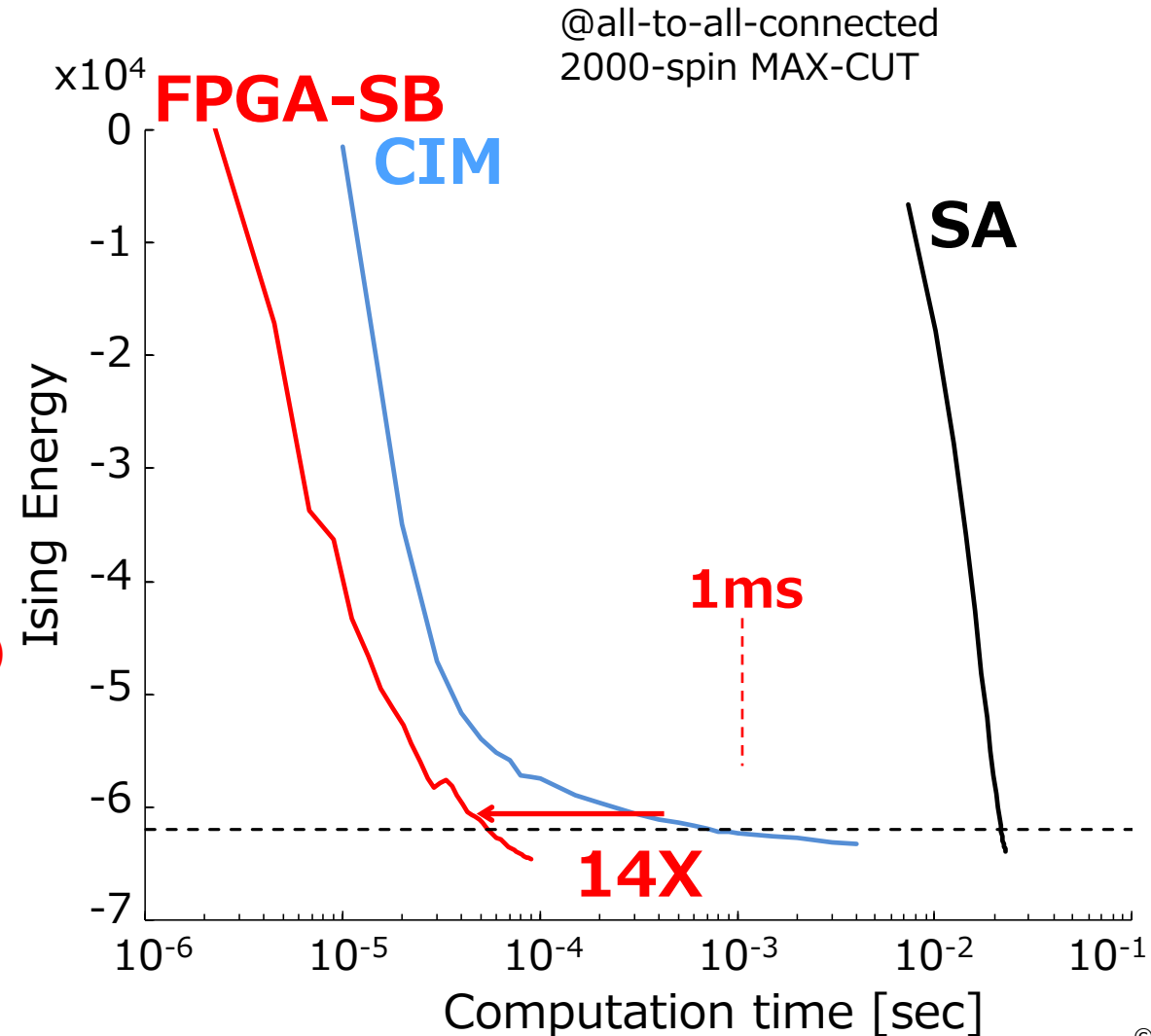
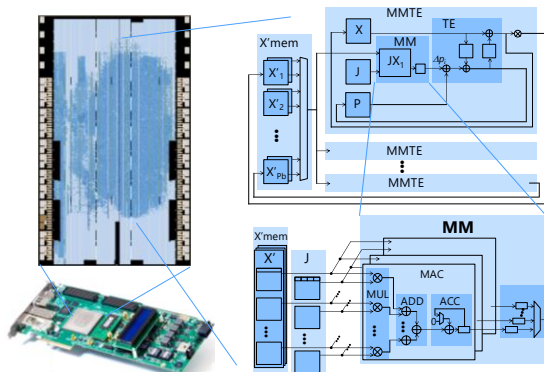
Faster and more efficient than the state-of-the-art one

Coherent Ising Machine 800 GMAC/s @ 1000 W



[T. Inagaki, Science 354, 603, '16]

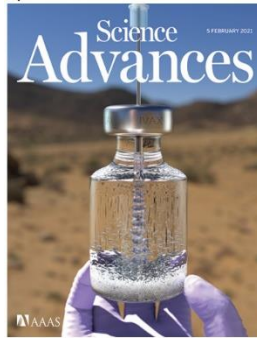
FPGA-SB 1,873 GMAC/s @ 49 W
(288X more energy efficient)



Performance*1 (2021)

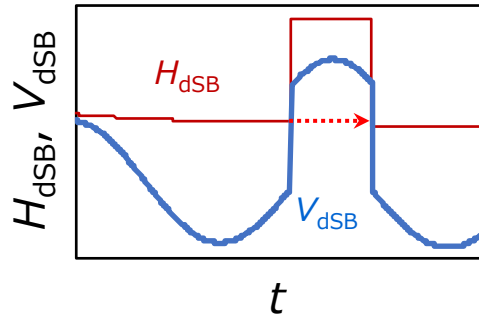
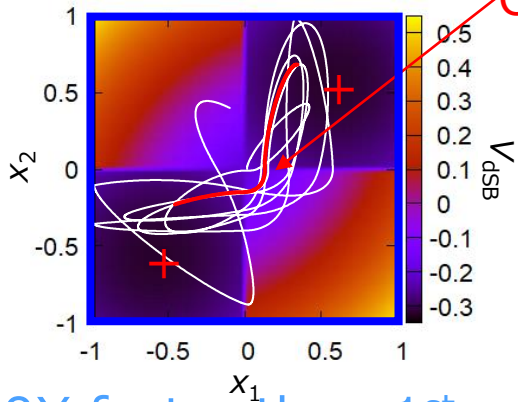
Comprehensive comparison →

Very competitive with state-of-the-art Ising machines

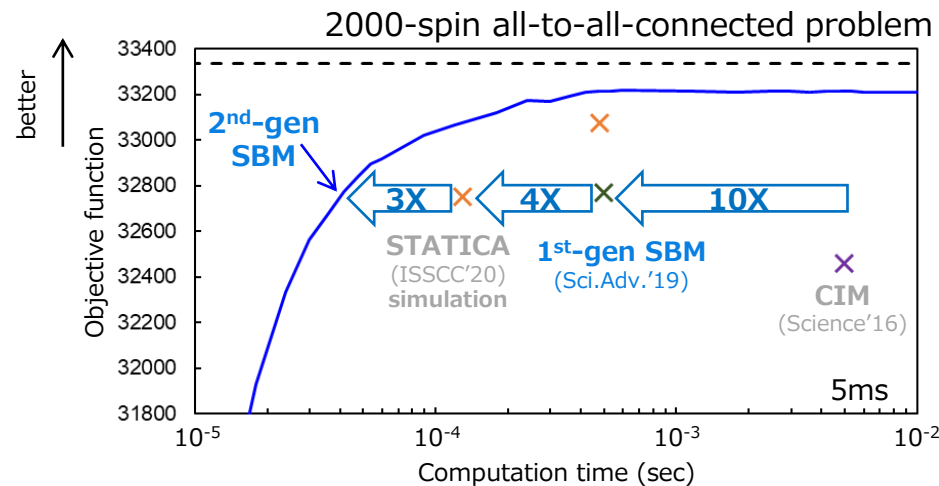


2nd-gen algorithm

Quasi-quantum tunneling



10X faster than 1st-gen



B

N	Connectivity	J_{ij}	Machine	TTT
2000 (K_{2000})	All-to-all	$\{\pm 1\}$	bSBM	0.26 ms
			STATICA	1.50 ms
			CIM	1.1 s
2000 (G22)	Sparse (1%)	$\{0, -1\}$	bSBM	0.11 ms
			CIM	14 ms

Bar chart showing TTT (s) on a logarithmic scale from 10^{-4} to 1. Red bars represent bSBM, and blue bars represent other machines.

C

N	Connectivity	J_{ij}	Machine	TTS
60	All-to-all	$\{\pm 1\}$	dSBM	9.2 μ s
			RBM	10 μ s
			CIM	0.6 ms
			QA	1.4 s
100	All-to-all	$\{\pm 1\}$	dSBM	29 μ s
			RBM	30 μ s
			SimCIM	0.6 ms
200	Sparse (Degree 3)	$\{0, -1\}$	dSBM	0.70 ms
			QA	11 ms
			CIM	51 ms
700	All-to-all	$\{\pm 1\}$	dSBM	25 ms
			SimCIM	0.14 s
			DA	0.27 s
1024	All-to-all	$\{\pm 1\}$	dSBM	55 ms
			DA	1 s
1024	All-to-all	16 bits $\{-2^{15} + 1, \dots, 2^{15} - 1\}$	dSBM	0.29 s
2000 (K_{2000})	All-to-all	$\{\pm 1\}$	dSBM	1.3 s
			DA	0.9 s
2000 (G22)	Sparse (1%)	$\{0, -1\}$	dSBM	2.7 s
			SimCIM	12 s

Bar chart showing TTS (s) on a logarithmic scale from 10^{-6} to 1. Red bars represent dSBM, and blue bars represent other machines.

Competitors

SB: Simulated bifurcation

QA: Quantum annealer

CIM: Coherent Ising machine

DA: Digital annealer

SimCIM: Simulated CIM

RBM: Restricted Boltzmann machine

MA: Momentum annealing

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Application of SBMs*1

Simulated bifurcation machines

*1 Toshiba's website "SQBM+™"

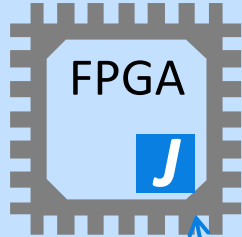
<https://www.global.toshiba/ww/products-solutions/ai-iot/sbm.html>

for Edge (high-speed real-time) and Cloud (large/wide-area)

edge/embedded

Lower latency

FPGA cluster






on-chip memory

J matrix

Single-shot processing

$$\begin{bmatrix} \Delta p_1 \\ \Delta p_2 \\ \square \\ \square \\ \square \end{bmatrix} = \begin{bmatrix} j_{11} & j_{12} & \square & \square & \square & \square \\ j_{21} & j_{22} & \square & \square & \square & \square \\ \square & \square & \square & \square & \square & \square \\ \square & \square & \square & \square & \square & \square \\ \square & \square & \square & \square & \square & \square \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \square \\ \square \\ \square \end{bmatrix}$$

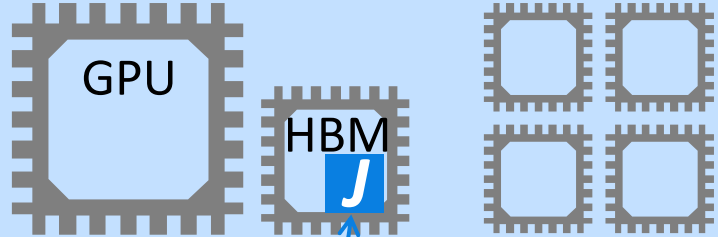
High-speed real-time systems

Financial trading   Autonomous control 

cloud

Larger problem

GPU cluster





off-chip memory

J matrix

Batch processing

$$\begin{bmatrix} \Delta p_1 & \Delta p_1 \\ \Delta p_2 & \Delta p_2 \\ \square & \square \\ \square & \square \\ \square & \square \end{bmatrix} = \begin{bmatrix} j_{11} & j_{12} & \square & \square & \square & \square \\ j_{21} & j_{22} & \square & \square & \square & \square \\ \square & \square & \square & \square & \square & \square \\ \square & \square & \square & \square & \square & \square \\ \square & \square & \square & \square & \square & \square \end{bmatrix} \begin{bmatrix} x_1 & x_1 \\ x_2 & x_2 \\ \square & \square \\ \square & \square \\ \square & \square \end{bmatrix}$$

Large/wide-area systems

Drug design  Planning 

Embeddable SBM

Simulated bifurcation machine

*1 K. Tatsumura et al., "FPGA-Based Simulated Bifurcation Machine," *IEEE Field-Programmable Logic and Apps. (FPL)*, 2019

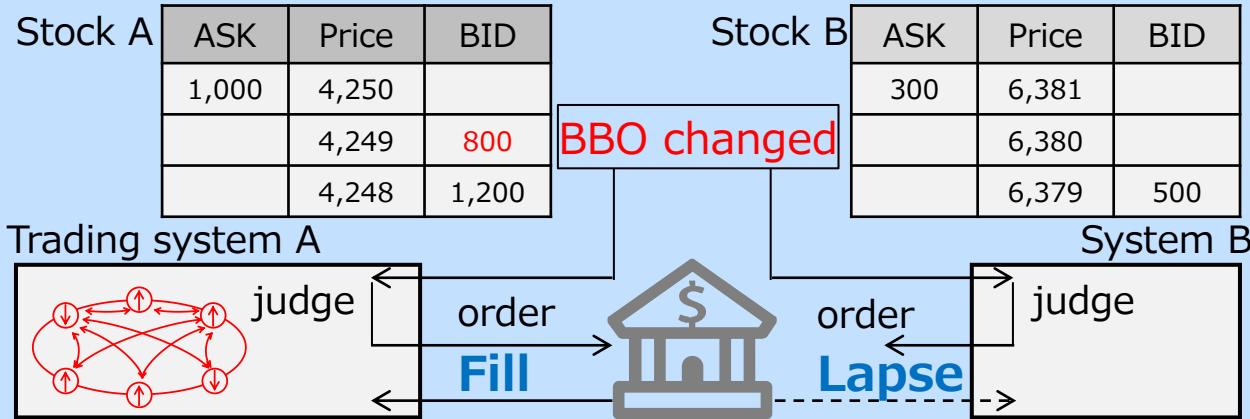
*2 K. Tatsumura, "Large-scale combinatorial optimization in real-time systems by FPGA-based accelerators for simulated bifurcation," *Int'l Symp. on Highly Efficient Accelerators and Reconfigurable Technologies (HEART)*, 2021

Enabling NP-hard optimization in real-time systems

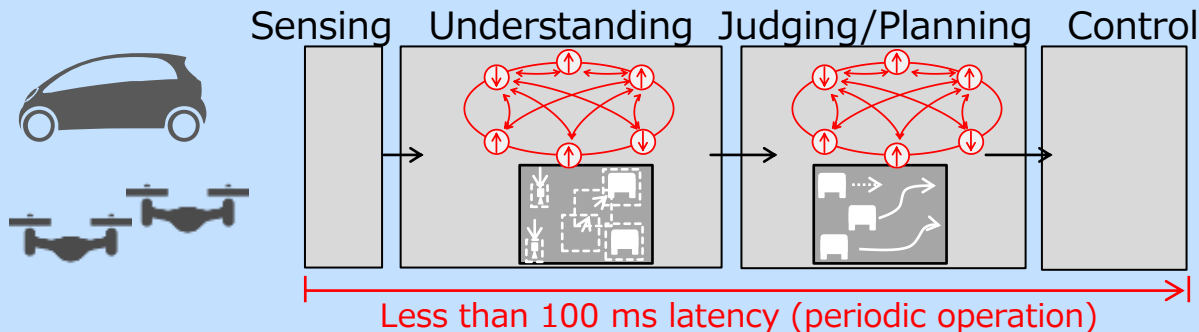
rational judgment

High-speed real-time systems

Financial trading system



Autonomous control

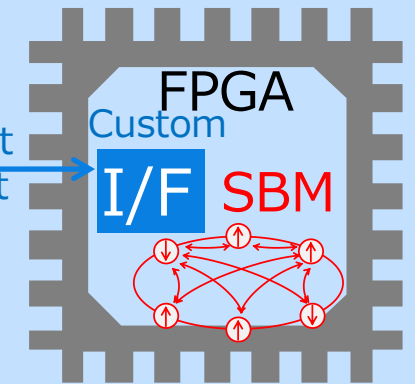


FPGA-based SBMs

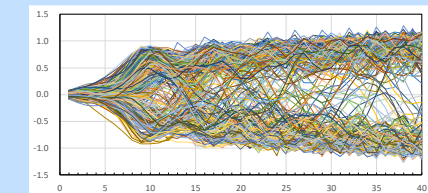
Ultralow latency (sub-msec)
Deterministic latency



Market packet



1. Embeddable
2. Custom I/F
3. SBM custom circuit (No software interrupt)



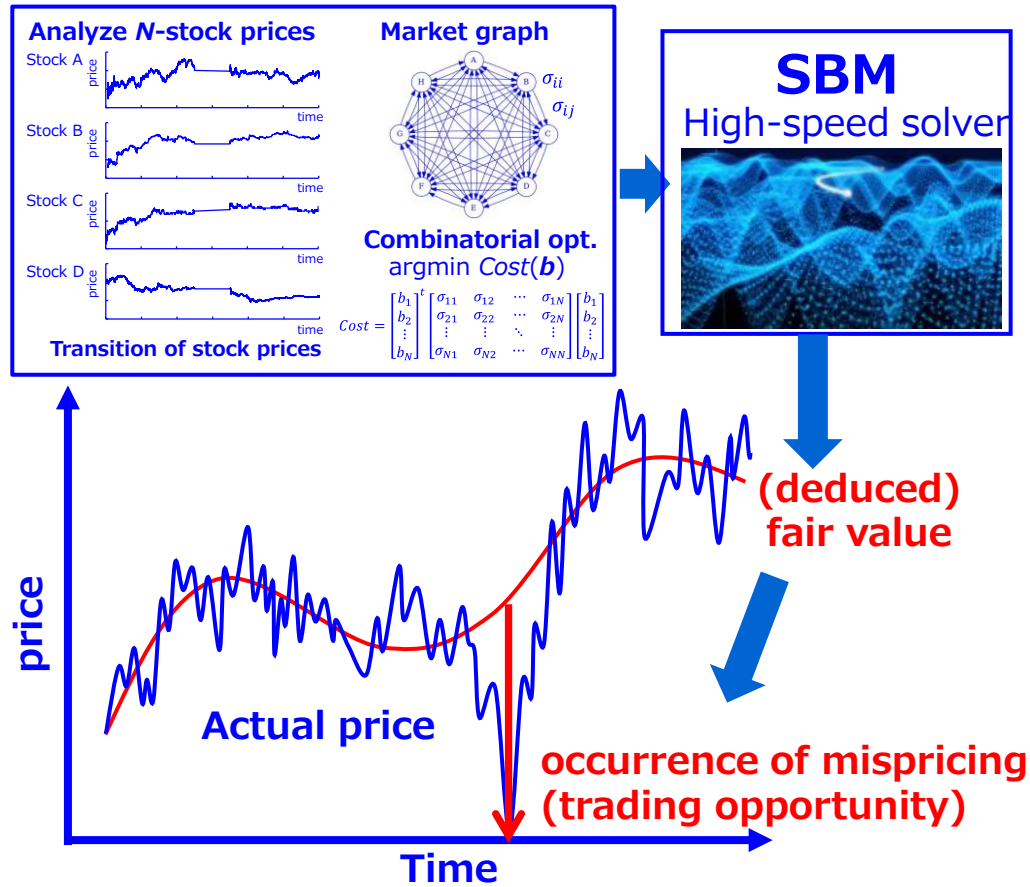
Applications in Finance

#1 [The world's first demonstration of systems that execute unprecedented stock trading strategies based on computationally-hard quadratic discrete optimization by using quantum-inspired computer](https://doi.org/10.1109/ACCESS.2020.9181114)

*1 <https://doi.org/10.1109/ACCESS.2023.3316727>
 *2 <https://doi.org/10.1109/ACCESS.2023.3326816>
 *3 <https://doi.org/10.1109/ACCESS.2023.3341422>

New strategies based on detection of ever-untargeted trading opportunities by SBMs

Even if your strategy is splendid, if there is a competitor executing the same one, you may lose
 Traders are essentially *technology-hungry*, pursuing a new strategy by new technologies



Type	High-speed real-time trading			Asset management
Target	Currency	Stock		
Strategy	Cross-currency arbitrage*1	Extended pair-trade*2	High-speed basket trade*3	Correlation-diversified portfolio*4
Opt.	Optimal path search in market graph	Optimal path search in market graph	Discrete portfolio optimization	Maximum independent set
Paper				
Publish	Oct. 12, 2020	Sep. 18, 2023	Oct. 23, 2023	Dec. 12, 2023

System -High-speed basket trade*1-

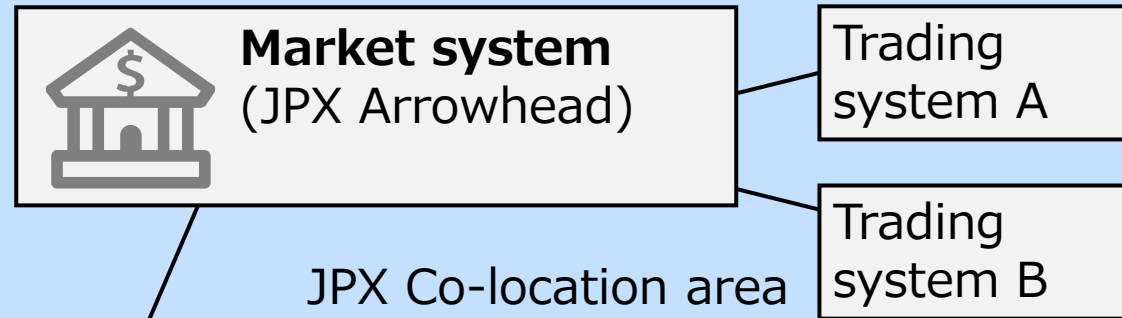
Real-time trading system with embedded SBM (164μs latency), installed at the JPX Co-location area of the TSE

special area for high-speed trading

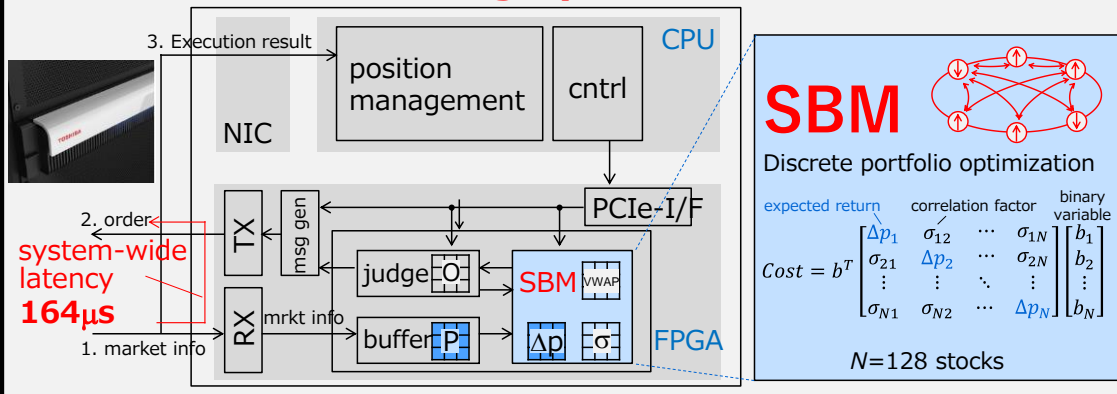
TOKYO Stock Exchange

System configuration

In a data center

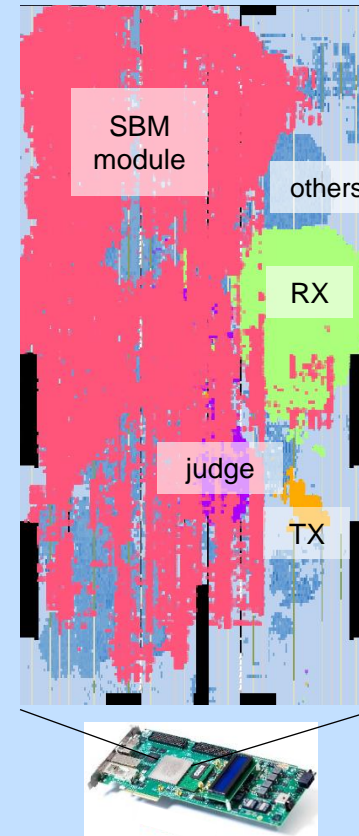


SBM real-time trading system



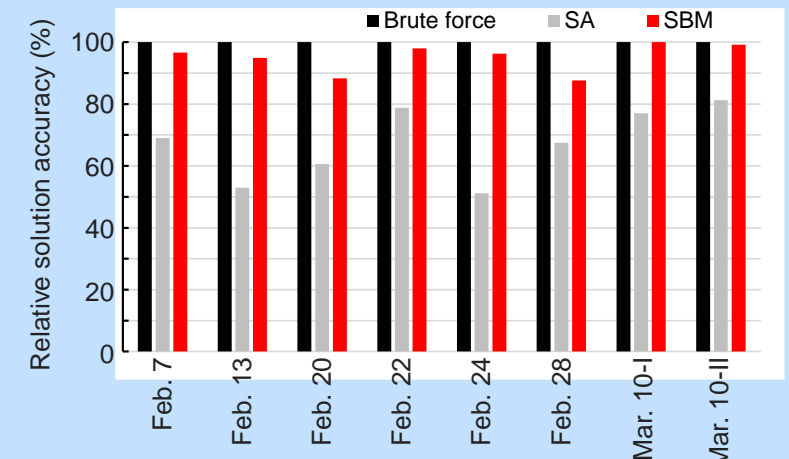
Embedded SBM

FPGA



SB alg. ver	Ballistic SB (bSB)
Machine size	Fully-connected 128 spins
Comp. precision	32-bit FP
Time per SBM run	162 μS

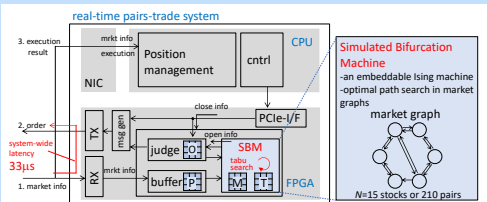
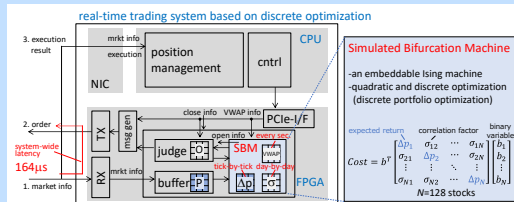

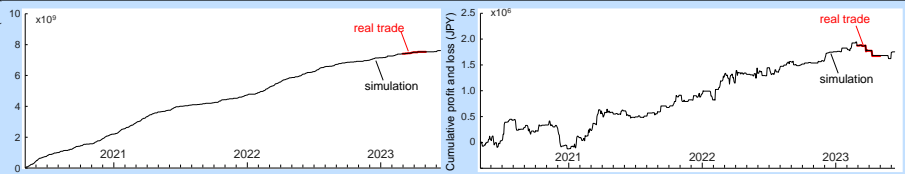
Single-shot solution accuracy



Market situations from Feb. 7, 2023 to Mar. 10, 2023

Demonstration at the Tokyo Stock Exchange

Execution capability of NP-hard optimization-based trading strategy through real-time/real-money transactions

Strategy & System	<h3>Extended pair-trade*1</h3>  <p>Optimal path search in market graph (a tabu search)</p>	<h3>High-speed basket trade*2</h3>  <p>Discrete portfolio optimization</p>
Real-time transactions vs. backsimulation assuming 100% fill rate <i>Execution at intended prices & volumes</i>	 <p>Good agreement → Proof of the execution capability in terms of speed</p>	 <p>Good agreement → Proof of the execution capability in terms of speed</p>
System-wide latency	33 μSEC for 210-pair universe	164 μSEC for 128-stock universe
Sharpe ratio (annualized return/risk)	0.79 (=7.5% / 9.5%)	1.23 (=3.6% / 2.9%)
Cumulative amounts of transaction	3,817,201,458 JPY (Total) 4 billion JPY transactions, 1000-hour no-error operation, 118,956,828 JPY	
Real-time trading hours	125 days or 750 hours (No errors)	42 days or 252 hours (No errors)

Strategy –High-speed basket trade*1-

*1 K. Tatsumura et al., "Real-time Trading System based on Selections of Potentially Profitable, Uncorrelated, and Balanced Stocks by NP-hard Combinatorial Optimization," *IEEE Access* **11**, pp. 120023 - 120033 (2023).

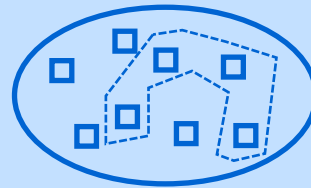
*2 VWAP: Volume-Weighted Average Price

Select a delta-neutral basket of stocks to maximize return and minimize correlation (risk) for improving Sharpe ratio

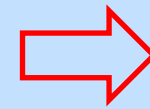
Formulation of QUBO

A typical "quadratic discrete optimization problem" (NP-hard)

Tradable stocks N ($N=128$)



Selection



Selected basket N_s

Binary variables

$$\mathbf{b} = [b_1 \ b_2 \ \dots \ b_N] \quad b_i \in \{0, 1\}$$

Unselected \swarrow Buy/Sell \nwarrow

Total cost function

$$H_{QUBO} = \sum_i^N \sum_j^N Q_{i,j} = H_{cost} + H_{penalty}$$

Cost

$$H_{cost} = [b_1 \ b_2 \ \dots \ b_N] \begin{bmatrix} \Delta P_1 & \sigma_{12} & \dots & \sigma_{1N} \\ \sigma_{21} & \Delta P_2 & \dots & \sigma_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ \sigma_{N1} & \sigma_{N2} & \dots & \Delta P_N \end{bmatrix} \begin{bmatrix} b_1 \\ b_2 \\ \vdots \\ b_N \end{bmatrix}$$

Penalty

$$H_{penalty} = c_2 \left(\left(\sum_i^N b_i \right) - N_s \right)^2 + c_3 \left(\sum_i^N \text{sgn}(\Delta p_i) b_i \right)^2$$

Maximize

Sum of expected return

Minimize

Sum of correlation factors (for diversified-portfolio)

Constrain I

Number of selected stocks, N_s

Constrain II

Delta neutral ($N_{buy} = N_{sell}$)



Applications in Automotive vehicle*1

*1 K. Oya et al., "Proposal and prototyping of automotive computing platform with Quantum inspired Processing Unit", Trans. of Society of Automotive Engineers of Japan 54, pp. 1216-1221 (2023). <https://doi.org/10.11351/jsaeronbun.54.1216>
<https://trid.trb.org/View/2270193>

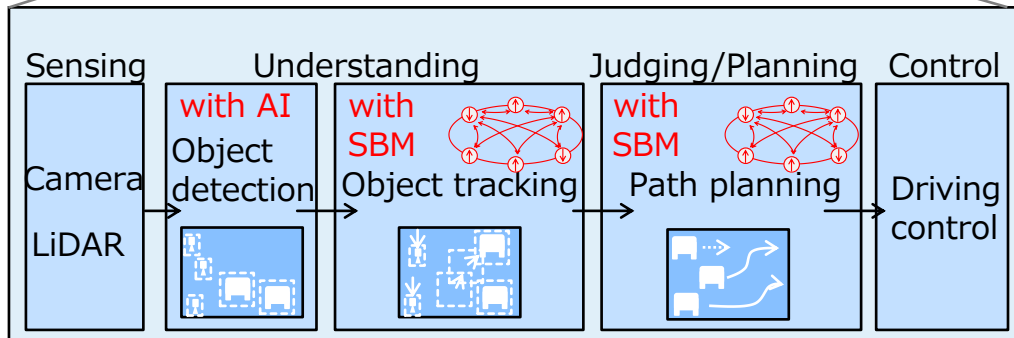
Toward autonomous car/driving-support tech that quickly and optimally respond to surrounding situation

Autonomous control systems: a typical mission-critical, high-speed, real-time system

Making understanding/judgment *more rational within critical time-constrains*



Autonomous control systems



Less than 100 ms latency (periodic operation)

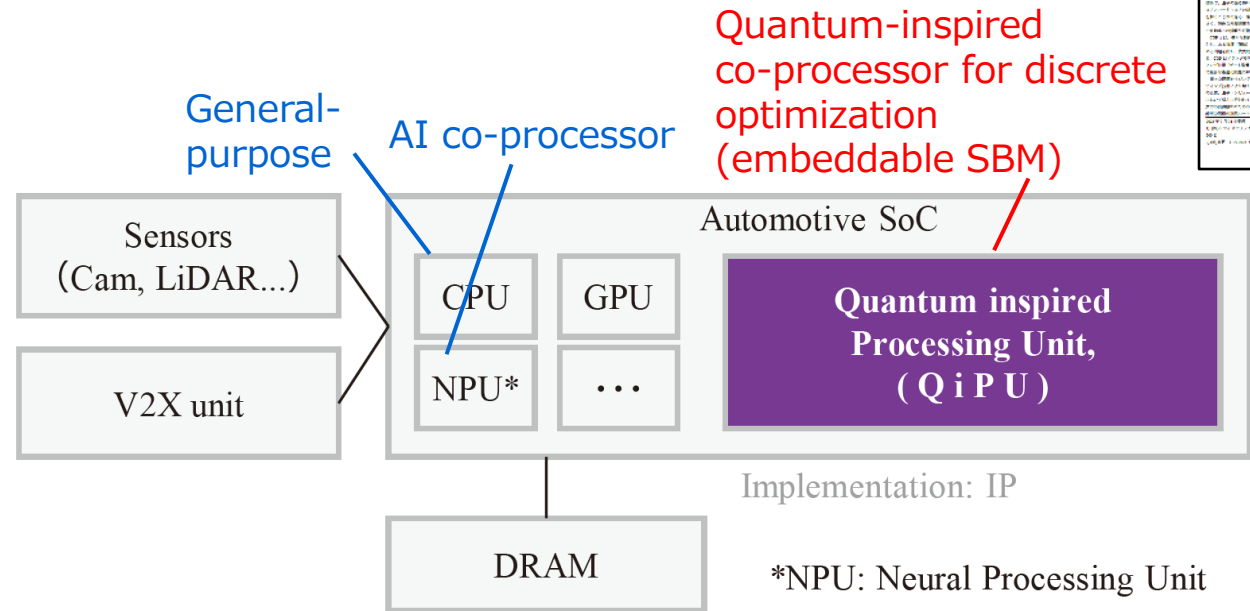


Fig.2 Architecture of automotive computing platform with Quantum inspired Processing Unit

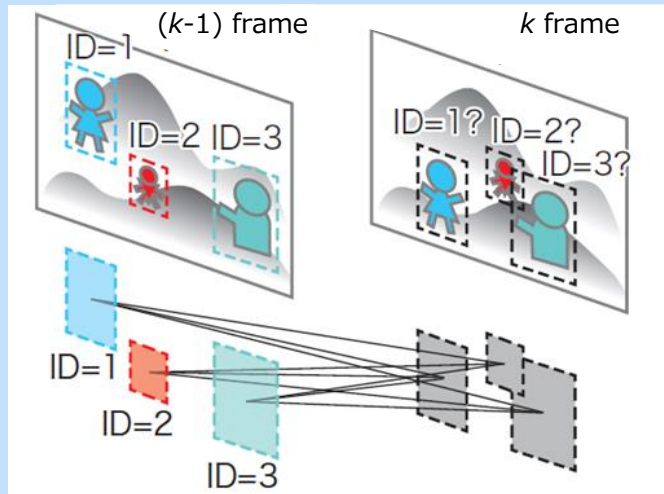
Multiple Object Tracking with **SBM***1

Simulated bifurcation machine

*1 K. Oya et al., "Proposal and prototyping of automotive computing platform with Quantum inspired Processing Unit", Trans. of Society of Automotive Engineers of Japan 54, pp. 1216-1221 (2023).
<https://doi.org/10.11351/jsaeronbun.54.1216>

Flexible matching functions by SBMs to realize tracking through multiple long-term occlusion events

Extended MOT



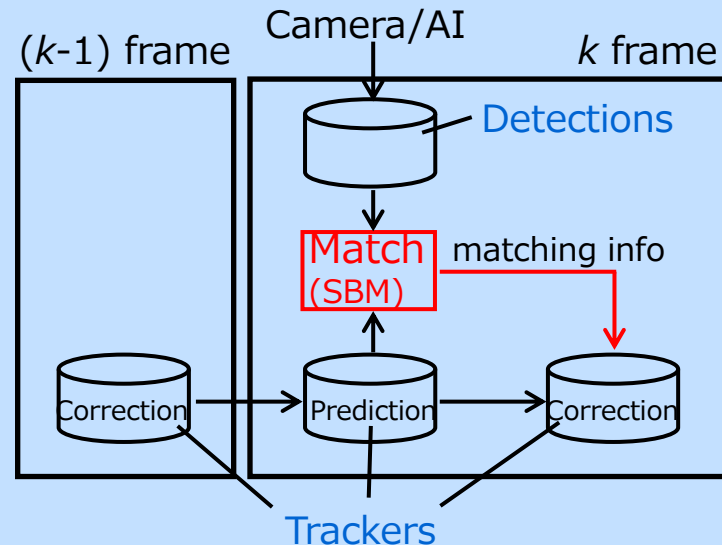
To realize tracking of objects through multiple long-term occlusion events

QUBO formulation

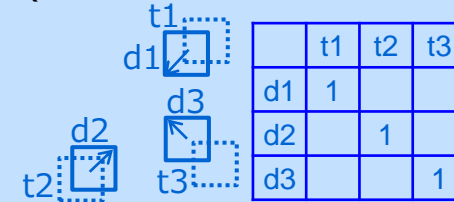
- Matching between *Detections* and *Trackers*
- Detect the occurrences & locations of occlusion events

- Execute SBM **twice** while changing the penalty weight (**c**) for prohibiting double-match

$$H_{QUBO} = \sum_i^N \sum_j^N Q_{i,j} = H_{\text{cost}} \setminus \text{Maximize intersections} + \mathbf{c} H_{\text{penalty}} \setminus \text{Prohibiting double-match}$$

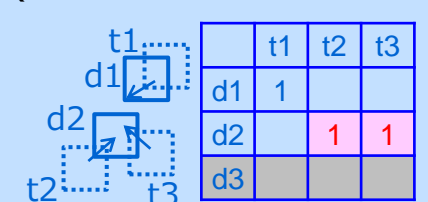


w/o occlusion
 (#Detections = #Trackers)



one-to-one matching

with occlusions
 (#Detections < #Trackers)



one-to-many matching

System throughput of 20 FPS and SBM-unique functions with vehicle-mountable FPGA boards

Vehicle-mountable boards

Detection (Segmentation by AI) Tracking (SBM)

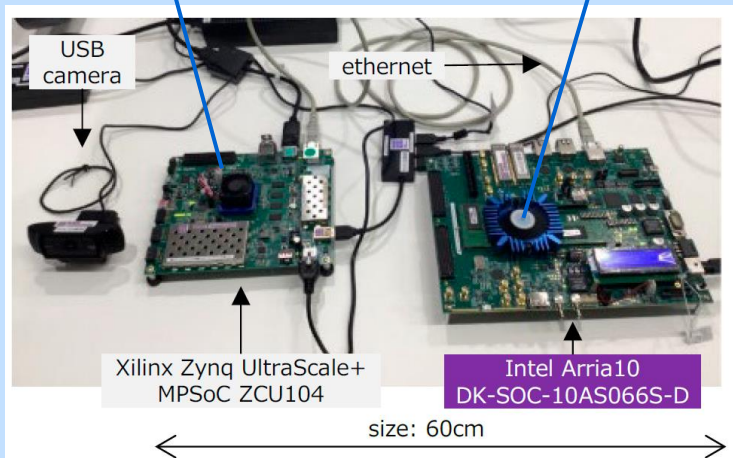


Fig.6 Appearance of prototype

SB alg. ver	Ballistic SB (bSB)
Machine size	Fully-connected 512 spins
# of MAC-PE	2,048
Time per SBM run	284 μ S

Throughput (>10FPS)

Table 3. Tracking performance of SORT with matching methods of Hungarian and SBM on MOT benchmark sequences⁽¹⁹⁾

MOT algorithm	Matching	MOTA \uparrow	HOTA \uparrow
Original SORT	Hungarian	48.77	44.80
Original SORT	SBM	48.76	44.83



Rectangles indicates Detection result, and Vectors in Rectangles indicates Tracking result.
 *This image is processed for privacy protection.

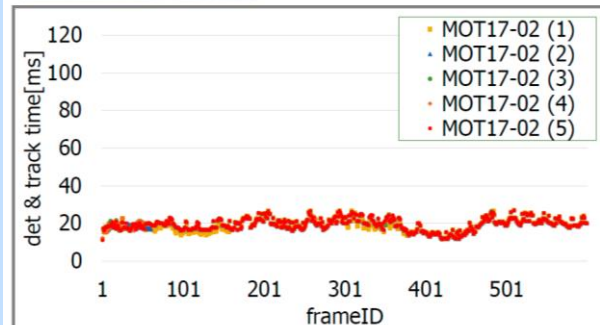


Fig.7 Evaluation result of processing time of prototype

System throughput of approx. 20 FPS

SBM-unique function

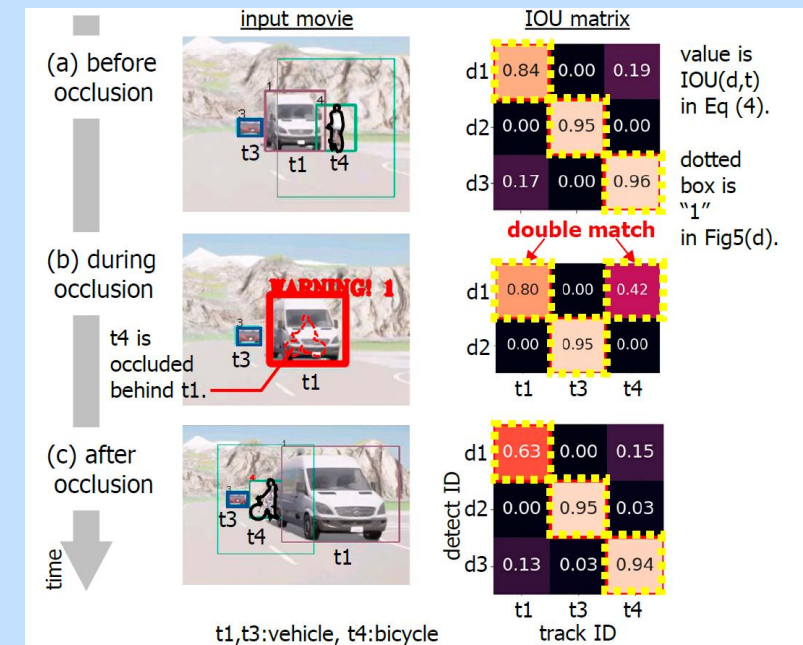


Fig.8 Function demonstration result of tracking through occlusion

Flexible matching functions for tracking through multiple long-term occlusion events

Simulated bifurcation machines

Simulated bifurcation (SB):

- quantum-inspired, highly-parallelizable algorithm for combinatorial optimization
- Can be accelerated with FPGAs/GPUs/NPUs → Very practical

High-speed real-time systems that make more rational judgments

- enabled by embeddable SBMs, for *innovative applications*

Demonstration

Financial trading

Execution capability of NP-hard optimization-based trading strategy through real-time/real-money transactions

Automotive vehicle

System throughput of 20 FPS (frames per second) and SBM-unique functions with vehicle-mountable FPGA boards

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- Scaled to **10M** variables and 1 Billion non-zero variables in QUBO arrays
- Increased to **3** new solvers (PUBO, QPLIB) on top of QUBO
- Increased to **4** algorithms (was 2), well-balancing accuracy and speed
- Support **3** AWS GPU types (p3, p4 and g4dn series)

Now available on Microsoft Azure
SQBM+™ V2

- Up to **10M** variables and 1 Billion non-zero variables in QUBO arrays
- Built-in **3** solvers (PUBO, QPLIB, QUBO)
- Essential **4** algorithms, well-balancing accuracy and speed
- Support **3** GPU Virtual Machines (V100, A100 and T4)

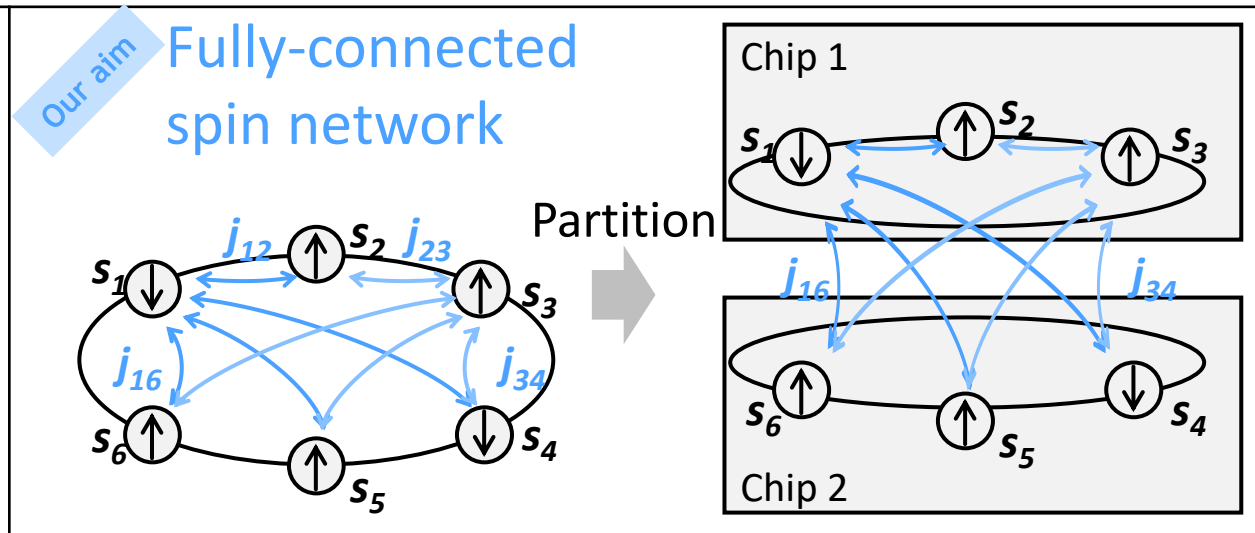
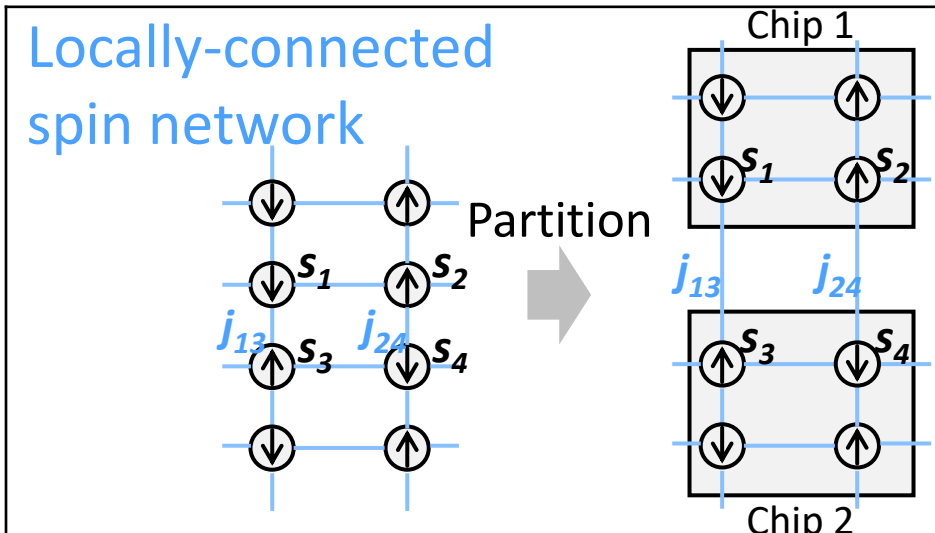
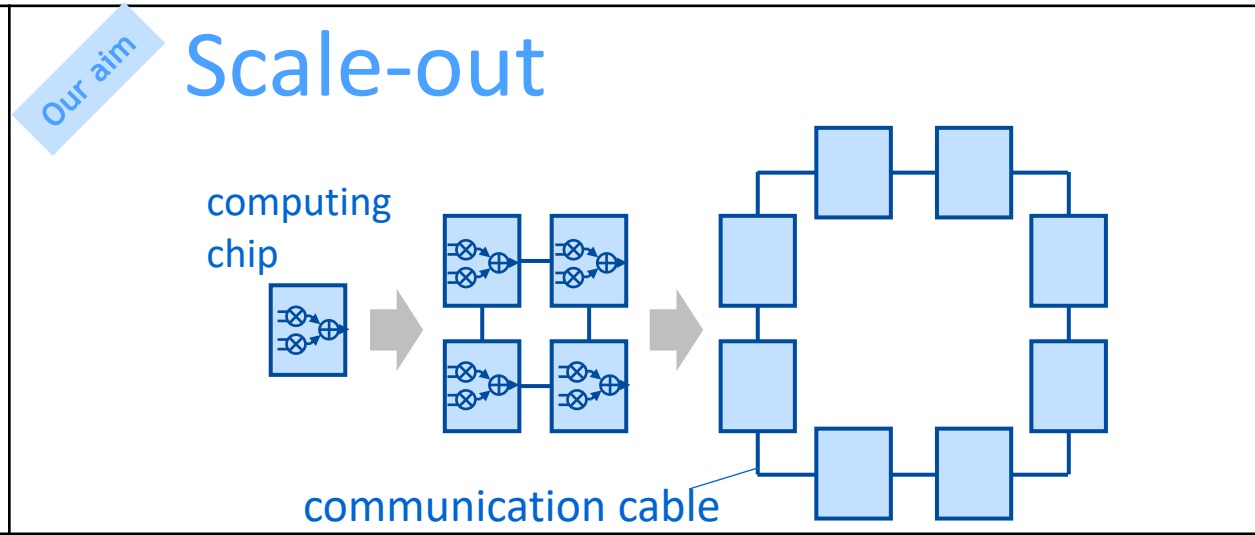
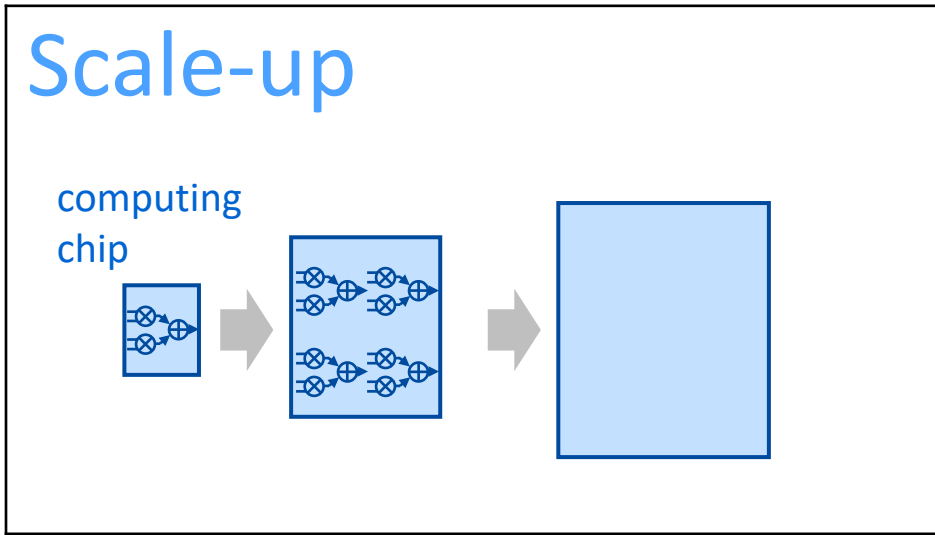
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Appendix

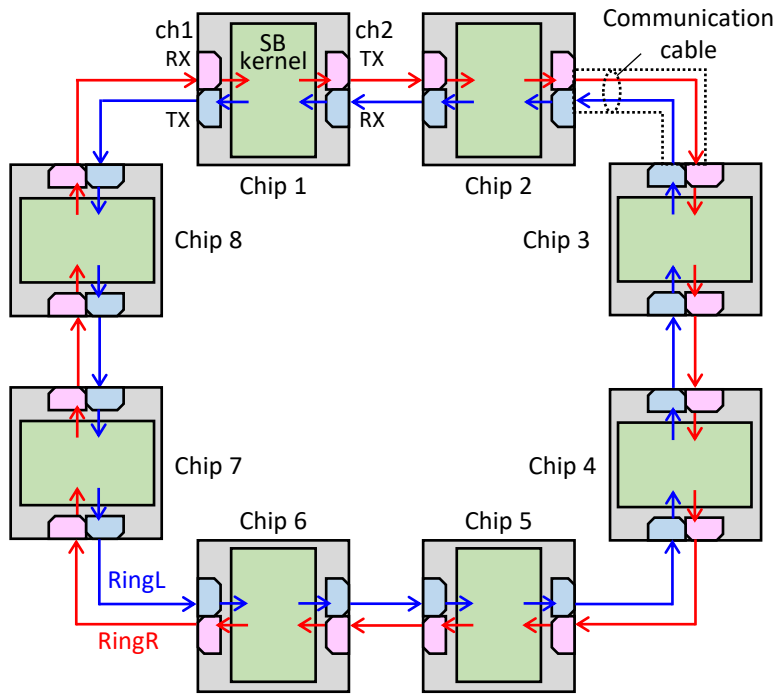
Appendix

Scaling out Ising machines with full spin-to-spin connectivity

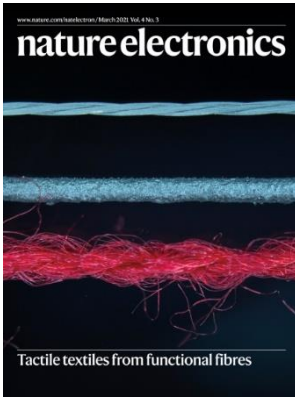
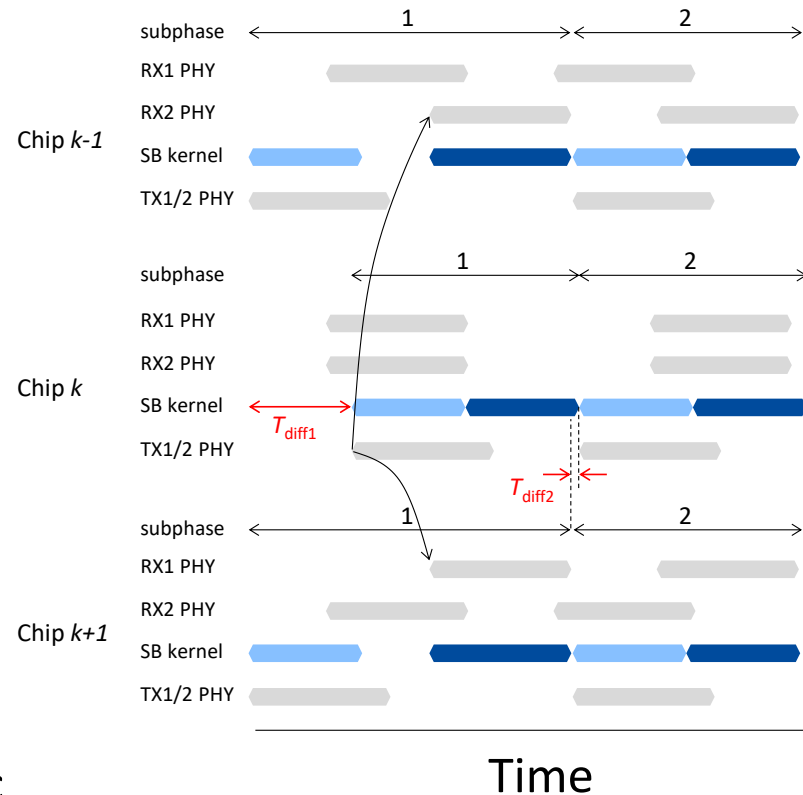


Multi-chip architecture based on partitioned SB

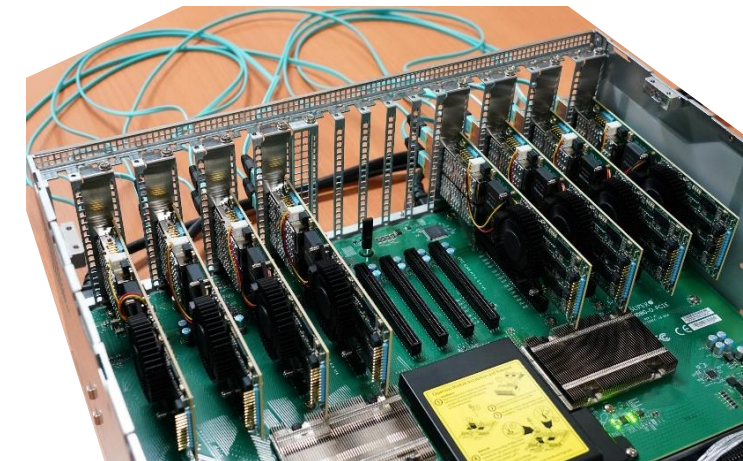
Bidirectional ring-network cluster without any centralized features



Autonomous synchronization mechanism (No clock-sharing, No central-HUB)



$P_{chip}=8$



All chips are autonomous, homogeneous and symmetric

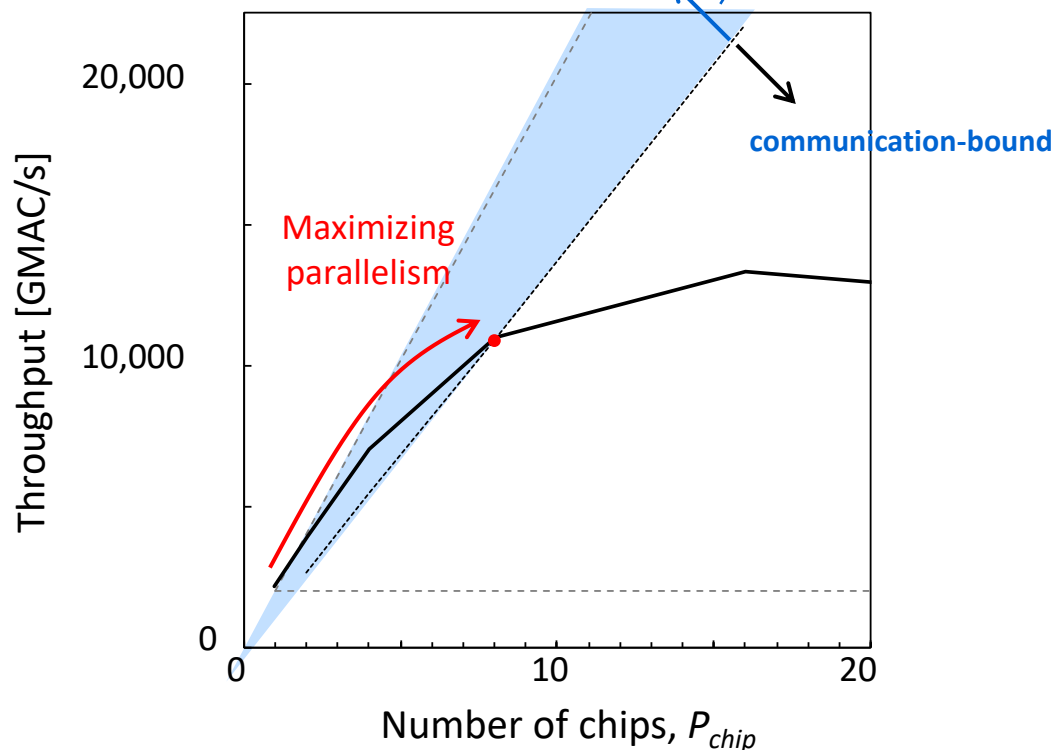
Good strong-scaling & weak-scaling characteristics

Strong scaling

Increase P_{chip} at a fixed problem size (N)

Computation-bound

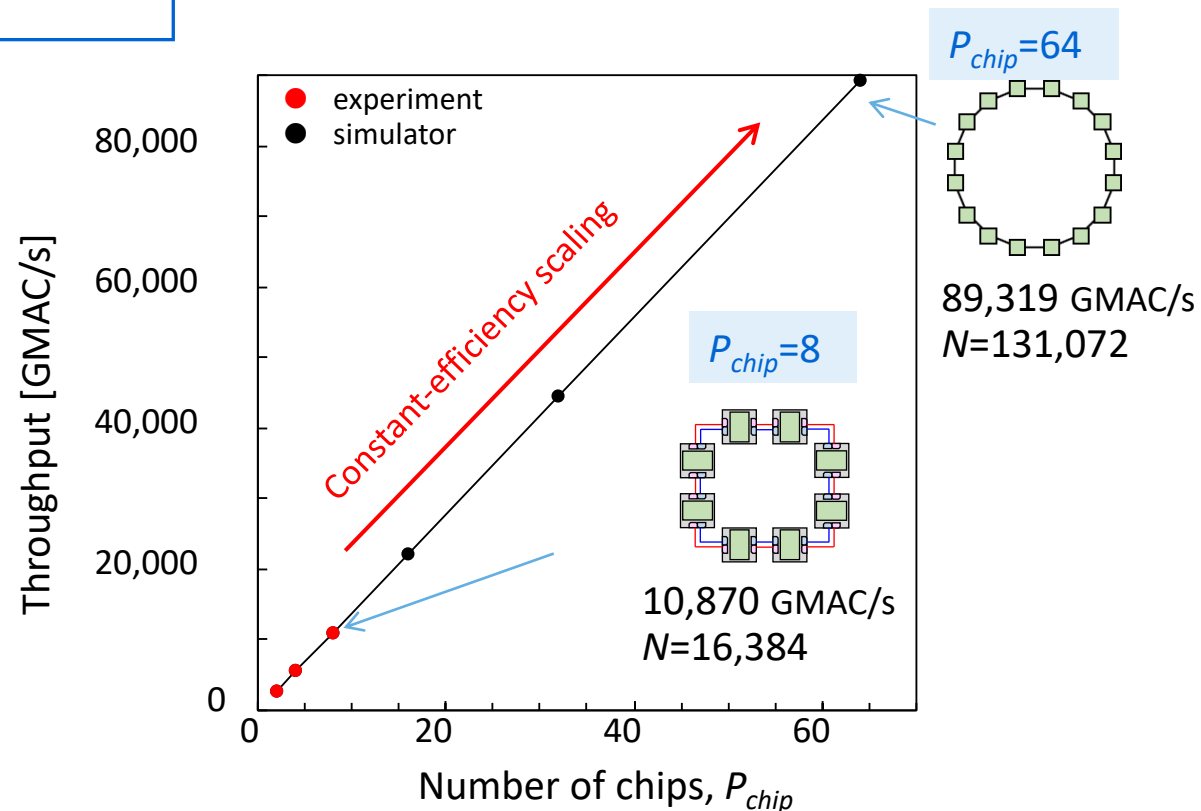
$$\frac{T_{computation}}{T_{communication}} > 1$$



Throughput enhancement **to the vicinity of an ideal upper limit** determined by the communication tech.

Weak scaling

Increase P_{chip} and N in the same proportion

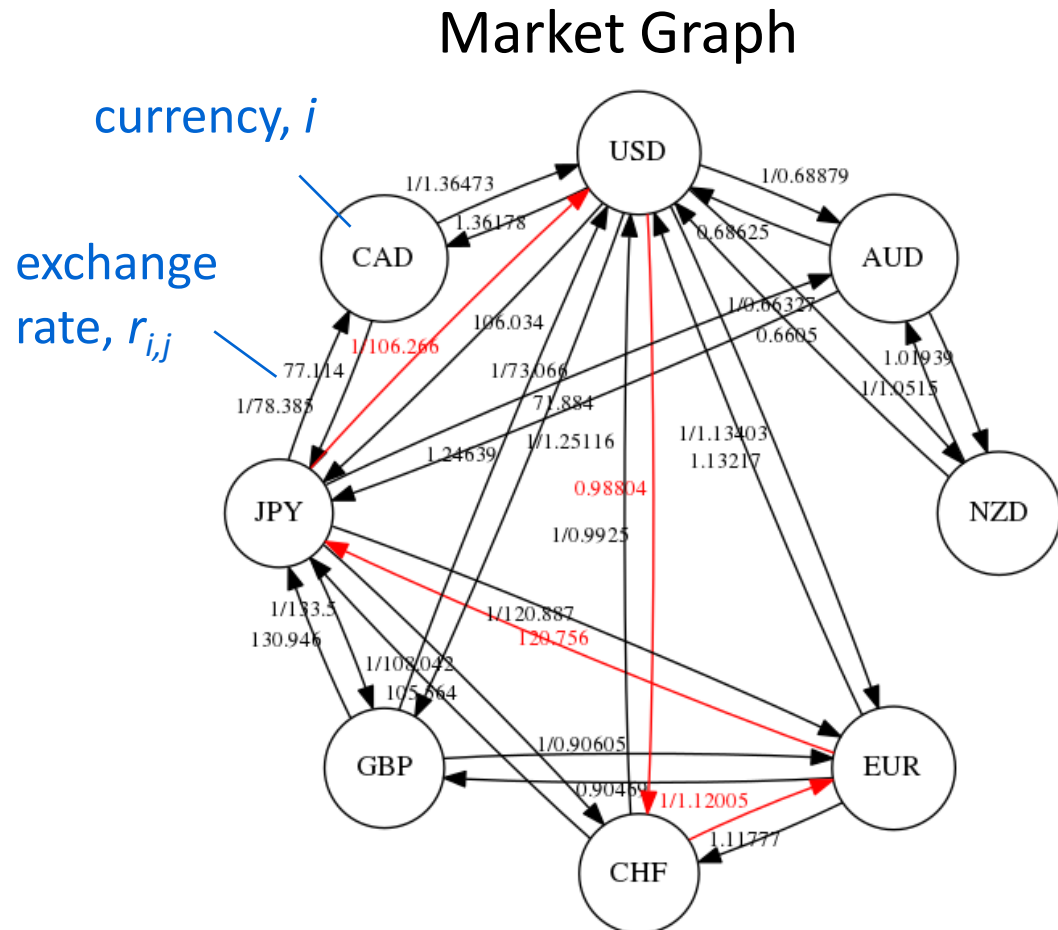


Constant-efficiency scaling **at the maximized computation parallelism (at the strong scaling limit)**

High-speed real-time trading

Trading system for cross-currency arbitrage*1

Optimal path search in a directed graph (a typical combinatorial problem)



Arbitrage Problem

find a closed path
that maximizes the profit

Cost function

$$Profit = \prod_{i,j \in \text{path}} r_{i,j}$$

Constraint

Must be
a closed path

Ising (QUBO) formulation

$$C_{tot} = m_c C + m_p P$$

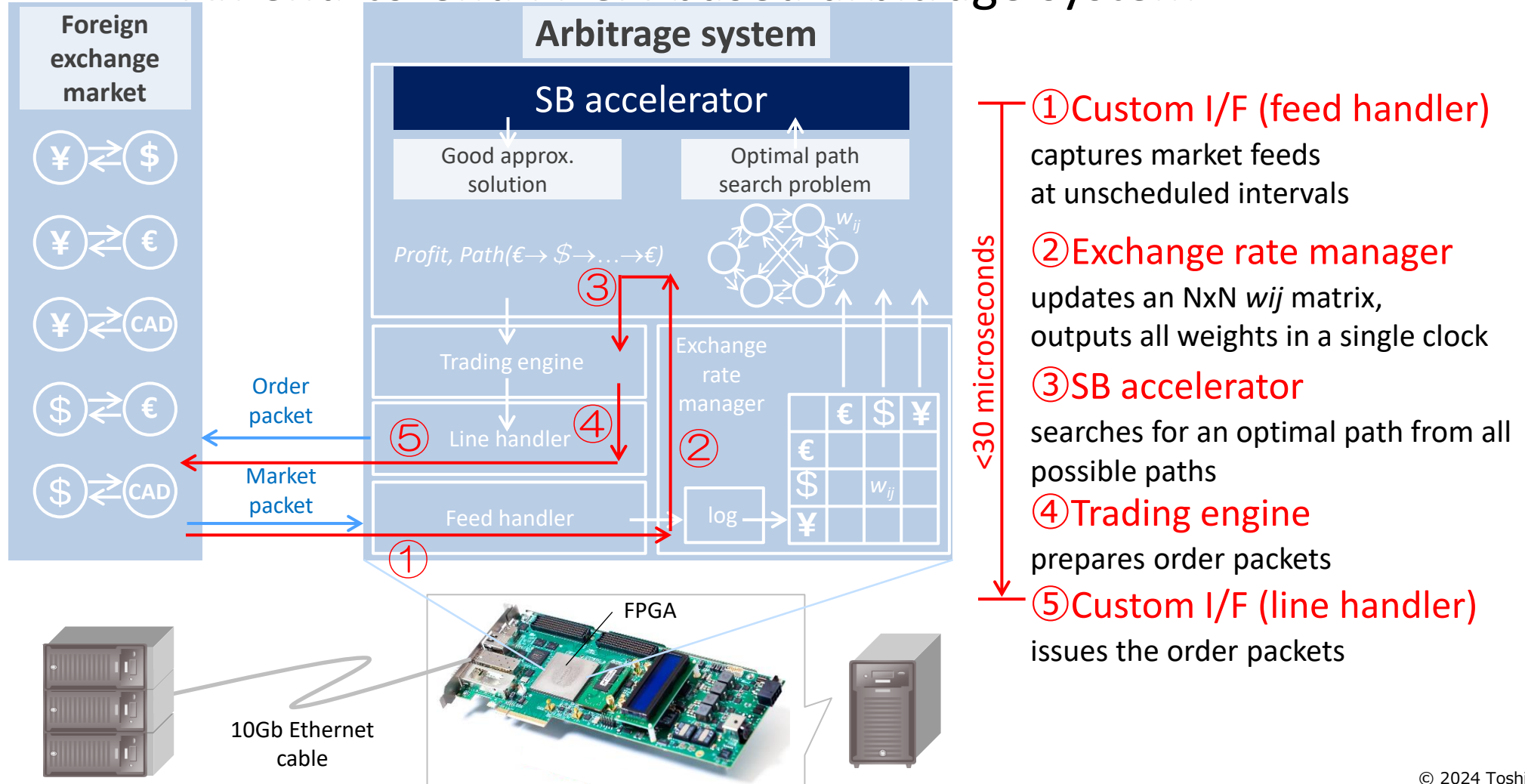
$$C' = \prod r_{i,j}^{b_{i,j}} \xrightarrow{w_{i,j} = -\log r_{i,j}} C = \sum w_{i,j} b_{i,j}$$

$$P = \sum_i \sum_{j \neq j'} b_{i,j} b_{i,j'} + \sum_j \sum_{i \neq i'} b_{i,j} b_{i',j} + \sum_i \left(\sum_j b_{i,j} - \sum_j b_{j,i} \right)^2 + \sum_{i,j} b_{i,j} b_{j,i}$$

High-speed real-time trading

Trading system for cross-currency arbitrage*1

An end-to-end FPGA-based arbitrage system

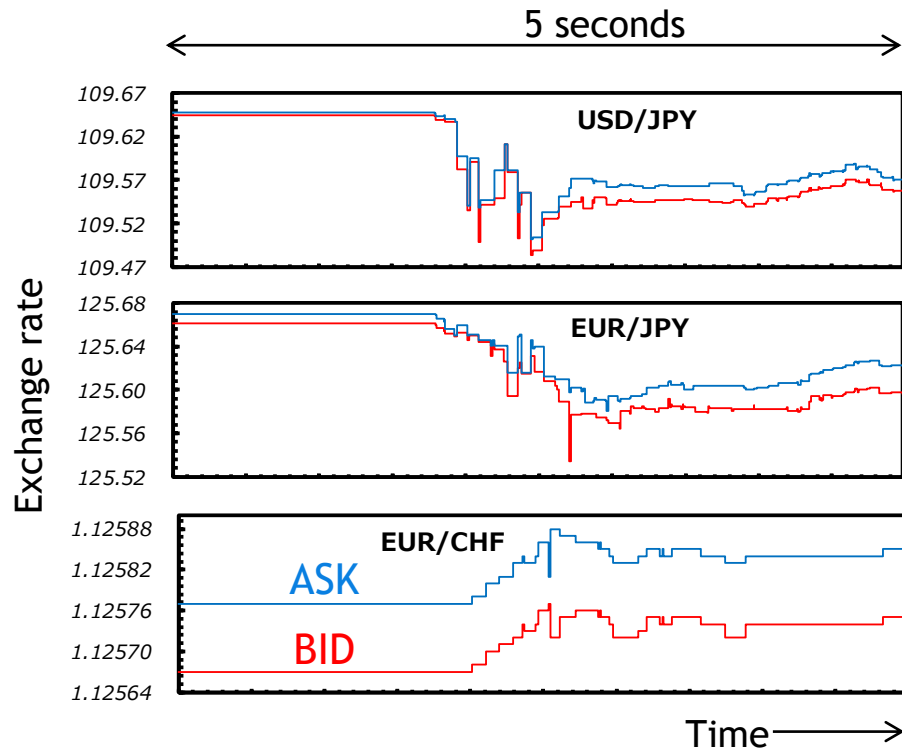


High-speed real-time trading

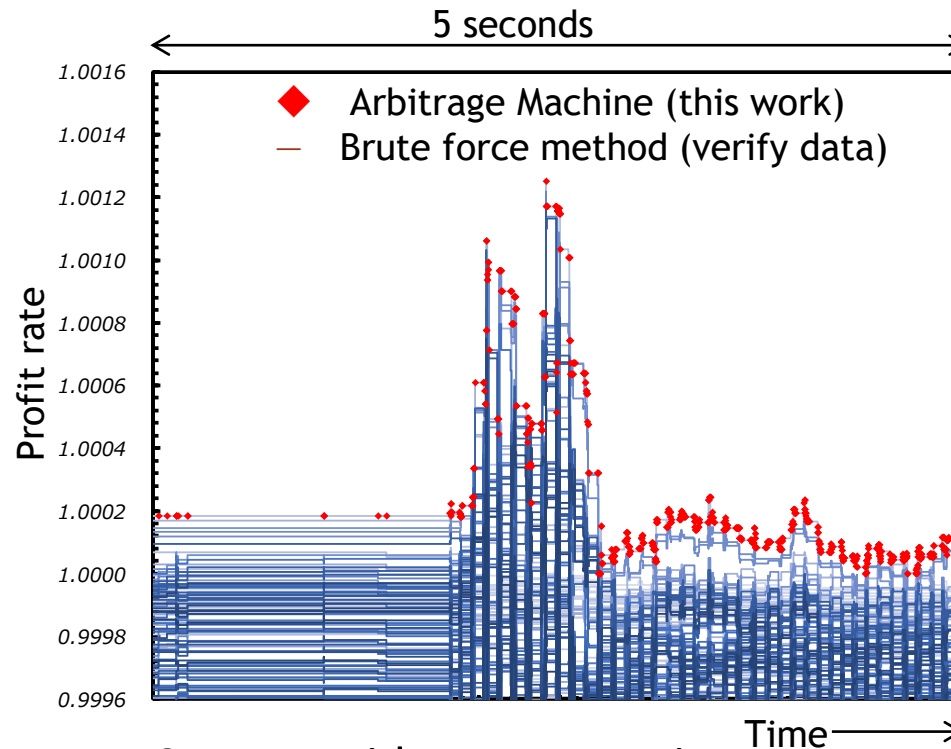
Trading system for cross-currency arbitrage*1

<30 μ s system-wide latency & 91% Top-1 probability

Exchange rates on Jan. 2nd, 2019



Profit rates for arbitrage paths



System-wide response time:
27.5 μ s (on average over 1000 packets)

Solution accuracy

